



Safe Testing with optimally GRO(W)ing e-values
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Abstract:

There has been significant recent progress on a new theory of hypothesis testing. The core of the new approach is the abstract concept of e-values, also known as betting scores. In this talk we focus on the question: "what is a good e-value?", for completely general testing problems with composite null and alternatives. Surprisingly, optimal Growth-Rate Optimal in Worst case "GROW" e-values, which lead to fastest capital growth, are fully characterised by the joint information projection (JIPr) between the set of all Bayes marginal distributions on H_0 and H_1 . We also discuss the related notion of Growth-Rate Optimal "GRO" (without the W), in case there is additional information about H_1 , or this can be learned from the data. As examples we show the GRO(W) e-value equivalent of the classical t-test and Fisher's exact test for 2x2 contingency tables.

Keywords:

hypothesis testing; e-values; betting scores; information projection

1. Introduction:

There has been significant recent progress on a new theory of hypothesis testing. The core of the new approach is the abstract concept of e-values, also known as betting scores. E-values are easier to interpret than classical p-values, behave well under optional continuation, and are easy to combine. E-values are closely connected to non-negative martingales and Bayes factors.

In this talk, part of the session on e-values, we focus on the question "what is a good e-value?". We introduce the GRO(W) criterion to characterize e-values that are in some sense optimal.

2. Methodology:

Surprisingly, the GROW e-values can be fully characterized by the joint information projection (JIPr) between the set of all Bayes marginal distributions on H_0 and H_1 .

3. Result:

We develop GRO(W) e-values for completely general testing problems with composite null and alternatives.

4. Discussion and Conclusion:

We introduce the GRO(W) criterion for characterising e-values that are in some sense optimal. We discuss the GRO(W) e-value equivalents of the classical t-test and Fisher's exact test for 2x2 contingency tables. We show that they perform competitively.

References:

1. Safe Testing - Peter Grünwald, Rianne de Heide, Wouter M. Koolen.

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FOR THE PAPER IS SIX PAGES**